



# *Tax and Efficiency Adjustments*




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## *Outline*

- Tax rate Adjustment
  - ALL tax rates defined as variables
  - ALL tax rates have a common adjustment mechanism
    - Multiplicative changes
    - Additive changes
- Efficiency changes
  - ALL efficiency factors defined as variables
  - ALL efficiency factors have a common adjustment mechanism
    - Multiplicative changes
    - Additive changes
- Hence, we have added a lot of variables – some without equations



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## *Why add so many variables?*

- We can only shock parameters
- Additional variables allow us to
  - change multiple parameters with one target
    - e.g., change ALL tariffs for a target internal balance and/or identify optimal tax rates
  - simplify the coding of simulations
  - **BUT** it makes the code less transparent
- This method means that we have
  - endogenous ‘variables’ – **flexed** in the closure
  - exogenous ‘variables’ – **fixed** in the closure



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## *Tax Rate Adjustment*



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## Import Duties

TMDEF (w, c, r) \$cmr (w, c, r) . .

TM (w, c, r) =E= { (tmb (w, c, r) + dabtm (w, c, r)) \* TMADJ (r) }  
+ {DTM (r) \*tm01 (w, c, r) } ;

- $tmb_{w,c,r}$  - vector of import duties in the base solution.
- $dabtm_{w,c,r}$  - vector of absolute changes in the vector of import duties taxes – initial values ZERO.
- $TMADJ_r$  - region specific variable whose initial value is ONE (parameter).
- $DTM_r$  is a region specific variable whose initial value is ONE (parameter).
- $tm01_{w,c,r}$  - vector of zeros and non zeros – initial values ZERO.



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## Import Duties - Multiplicative

TMDEF (w, c, r) \$cmr (w, c, r) . .

TM (w, c, r) =E= { (tmb (w, c, r) + dabtm (w, c, r)) \* TMADJ (r) }  
+ {DTM (r) \*tm01 (w, c, r) } ;

- If  $TMADJ$  for one region is made a variable, then the solution value for  $TMADJ$  yields the optimum equiproportionate change in the import duty rates necessary to satisfy model constraints.



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## Import Duties - Multiplicative

```
TMDEF (w, c, r) $cmr (w, c, r) . .
  TM (w, c, r) =E= { (tmb (w, c, r) + dabtm (w, c, r)) * TMADJ (r) }
                  + {DTM (r) * tm01 (w, c, r) } ;
```

- If *TMADJ* for one region is made a variable, and any elements of *dabtm* are non zero, then the solution value for *TMADJ* yields the optimum equiproportionate change in the *applied* import duty rates, i.e.,  $(tmb + dabtm)$ .



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## Import Duties – Fixed Additive

```
TMDEF (w, c, r) $cmr (w, c, r) . .
  TM (w, c, r) =E= { (tmb (w, c, r) + dabtm (w, c, r)) * TMADJ (r) }
                  + {DTM (r) * tm01 (w, c, r) } ;
```

- If any element of *dabtm* is not zero, then an absolute change in the initial import duty rate for the relevant commodity and trade partner is imposed.




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## Import Duties – Additive

```


TMDEF (w,c,r) $cmr (w,c,r) . .
  TM(w,c,r) =E= { (tmb(w,c,r) + dabtm(w,c,r)) * TMADJ(r) }
                + {DTM(r)*tm01(w,c,r) } ;
  
```

- If *DTM* for one region is made a variable, and ALL elements of *tm01* are ‘ONE’ then ALL the elements of *tmb* increase (additively) by an equal absolute amount determined by the solution value for *DTM*.



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## Import Duties – Additive

```

TMDEF (w,c,r) $cmr (w,c,r) . .
  TM(w,c,r) =E= { (tmb(w,c,r) + dabtm(w,c,r)) * TMADJ(r) }
                + {DTM(r)*tm01(w,c,r) } ;
  
```

- If *DTM* for one region is made a variable, AND at least **one** element of *tm01* is ‘ONE’ then the subset of elements of *tmb* identified by *tm01* are allowed to (additively) increase by an equal absolute amount determined by the solution value for *DTM* so as to satisfy the model.



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## Import Duties – Additive

```
TMDEF(w,c,r) $cmr(w,c,r) . .
  TM(w,c,r) =E= { (tmb(w,c,r) + dabtm(w,c,r)) * TMADJ(r) }
                + {DTM(r)*tm01(w,c,r) } ;
```

- If the change in the applied tax rates is to be other than equal then values of *tm01* other than ‘one’ can be applied.
- Typically the values for *tm01* will be bounded by ZERO and ONE.



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## Model Variables & Equations

- Variables added to the model with equations
  - $T^{**}(\dots)$
  - $T^{**}DEF(\dots)$
- Variables added to the model w/o equations
  - $T^{**}ADJ(\dots)$
  - $DT^{**}(\dots)$
- Increases the number of variables that **must** be fixed



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## Commodity Taxes

```
TEDEF(c,w,r)$cer(c,w,r)..
  TE(c,w,r) =E= ((teb(c,w,r) + dabte(c,w,r))* TEADJ(r))
                + (DTE(r)*te01(c,w,r)) ;

TMDEF(w,c,r)$cmr(w,c,r)..
  TM(w,c,r) =E= ((tmb(w,c,r) + dabtm(w,c,r))* TMADJ(r))
                + (DTM(r)*tm01(w,c,r)) ;

TSDEF(c,r)$((cd(c,r) OR cm(c,r)) AND rgn(r))..
  TS(c,r) =E= ((tsb(c,r) + dabts(c,r))* TSADJ(r))
                + (DTS(r)*ts01(c,r)) ;

TVDEF(c,r)$((cd(c,r) OR cm(c,r)) AND rgn(r))..
  TV(c,r) =E= ((tvb(c,r) + dabtv(c,r))* TVADJ(r))
                + (DTV(r)*tv01(c,r)) ;
```



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## Activity Taxes

```
TXDEF(a,r)$rgn(r)..
  TX(a,r) =E= ((txb(a,r) + dabtx(a,r))* TXADJ(r))
                + (DTX(r)*tx01(a,r)) ;

TFDEF(f,a,r)$rgn(r)..
  TF(f,a,r) =E= ((tfb(f,a,r) + dabtf(f,a,r))* TFADJ(r))
                + (DTF(r)*tf01(f,a,r)) ;
```




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## *Direct Taxes*

```

TYFDEF(f,r)$rgn(r) ..
  TYF(f,r) =E= ((tyfb(f,r) + dabtyf(f,r))* TYFADJ(r))
               + (DTYF(r)*tyf01(f,r)) ;

TYHDEF(h,r)$rgn(r) ..
  TYH(h,r) =E= ((tyhb(h,r) + dabtyh(h,r))* TYHADJ(r))
               + (DTYH(r)*tyh01(h,r)) ;

```



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## *Efficiency factors*



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## Standard Format

ADXEQ(a,r) ..

$$ADX(a,r) = E = \{ (adx_b(a,r) + dabadx(a,r)) * ADXADJ(r) \} \\ + \{ DADX(r) * adx01(a,r) \} ;$$

- $adx_{a,r}$  - vector of efficiency parameters.
- $dabadx_{a,r}$  - vector of absolute changes in the vector of efficiency parameters – initial values ZERO.
- $ADXADJ_r$  - region specific variable whose initial value is ONE.
- $DADX_r$  is a region specific variable whose initial value is ZERO.
- $adx01_{a,r}$  - vector of zeros and non zeros – initial values ZERO.



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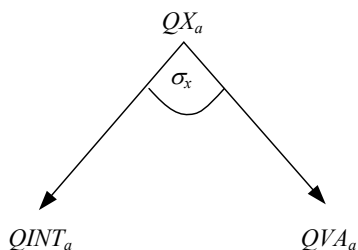
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## Production System – Sample Activity



QXPRODFN(a,r) \$(aqx(a,r) AND rgn(r)) ..

$$QX(a,r) = E = ADX(a,r) \\ * (deltax(a,r) * QVA(a,r) ** (-rhox(a,r)) \\ + (1-deltax(a,r)) * QINT(a,r) \\ ** (-rhox(a,r)) ** (-1/rhox(a,r)) ;$$



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## Top Level - Multiplicative

ADXEQ(a,r) ..

$$ADX(a,r) =E= \{ (adx_b(a,r) + dabadx(a,r)) * ADXADJ(r) \} \\ + \{ DADX(r) * adx01(a,r) \} ;$$

- If *ADXADJ* is made a variable, then the solution value for *ADXADJ* yields the optimum equiproportionate change in the top level efficiency factors necessary to satisfy model constraints.
- If *ADXADJ* is made a variable, and any elements of *dabadx* are non zero, then the solution value for *ADXADJ* yields the optimum equiproportionate change in the *applied* efficiency factors, i.e., *adx\_b + dabadx*.



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## Top Level - Additive

ADXEQ(a,r) ..

$$ADX(a,r) =E= \{ (adx_b(a,r) + dabadx(a,r)) * ADXADJ(r) \} \\ + \{ DADX(r) * adx01(a,r) \} ;$$

- If any element of *dabadx* is not zero, then an absolute change in the initial efficiency factors for the relevant activities are imposed.
- If *DADX* for one region is made a variable, and ALL elements of *adx01* are ONE then ALL the elements of *adx\_b* increase (additively) by an equal absolute amount determined by the solution value for *DADX*.
- If the change in the applied efficiency rates is to be other than equal then values of *adx01* other than one can be applied.



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## Value Added Production System

```

QVAPRODFN(a,r)$rgn(r) ..
QVA(a,r) =E= ADVA(a,r)
              *(SUM(f$deltava(f,a,r),deltava(f,a,r)
              *(ADFD(f,a,r)*FD(f,a,r))**(-rhova(a,r))))
              **(-1/rhova(a,r)) ;
  
```

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## Value Added Production System

```

ADVAEQ(a,r) ..
ADVA(a,r) =E= {(advab(a,r) + dabadva(a,r)) * ADVAADJ(r)}
              + {DADVA(r) * adva01(a,r)} ;
  
```

- If *ADVAADJ* for one region is made a variable, then the solution value for *ADVAADJ* yields the optimum equiproportionate change in the Second Level efficiency factors necessary to satisfy model constraints.
- If *ADVAADJ* for one region is made a variable, and any elements of *dabadva* are non zero, then the solution value for *ADVAADJ* yields the optimum equiproportionate change in the **applied** efficiency factors, i.e., *advab + dabadva*.
- If any element of *dabadva* is not zero, then an absolute change in the initial efficiency factors for the relevant activities are imposed.
- If *DADVA* for one region is made a variable, and ALL elements of *adva01* are ONE then ALL the elements of *advab* increase (additively) by an equal absolute amount determined by the solution value for *DADVA*.
- If *DADVA* for one region is made a variable, AND at least one element of *adva01* is ONE then the subset of elements of *advab* identified by *adva01* are allowed to (additively) increase by an equal absolute amount determined by the solution value for *DADVA* so as to satisfy the model.
- If the change in the applied efficiency rates is to be other than equal then values of *adva01* other than one can be applied.

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# Value Added Production System

The diagram shows a triangle with  $QVA_a$  at the top vertex. Inside the triangle is a circle containing  $\sigma_{va}$ . Three arrows point downwards from the triangle to the labels  $FD_{k,a}$ ,  $FD_{l1,a}$ , and  $FD_{l2,a}$ .

```
QVAPRODFN(a,r) $rgn(r) . .  
QVA(a,r) =E= ADVA(a,r)  
              *(SUM(f$deltava(f,a,r),deltava(f,a,r)  
                    *(ADFD(f,a,r)*FD(f,a,r))**(-rhoval(a,r))))  
                    **(-1/rhovl(a,r)) ;
```

Stock/flow relationship

No standard equation in the model

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# Tax and Efficiency Adjustments

## The End

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